

From the above figure we can obtain following equations.

$$\Delta\varphi'' = \frac{S \cdot \cos(A'_x + A_y) / 2}{M_M \sin l''}$$

$$\Delta\lambda'' = \frac{S \cdot \sin(A_y + A'_x) / 2}{N_M \cdot \cos\varphi_M \cdot \sin l''}$$

$$A'_x = A_y + \Delta A$$

$$\Delta A'' = \Delta\lambda \sin\varphi_m$$

The Inverse of mid latitude formula

The reverse method $\lambda_x, \varphi_x, \lambda_y, \varphi_y$ are our known data's S, A_y and A'_x should be found.

$$A_y + A'_x = 2 \tan^{-1} \left[\frac{\Delta\lambda'' \cdot N_M \cos\varphi_M}{\Delta\varphi'' M_M} \right]$$

$$\Delta A = \Delta\lambda \cdot \sin\varphi_m$$

$$S \cdot \sin(\alpha_{12} + \Delta\alpha/2) = N_m \cos\varphi_m \Delta\lambda$$

Hence, can calculate the A'_x, A_y , by using above answer; Now we can calculate the S by using above equations

(References : Erakiwsky E.J. , Thomson D.B. (1974) Geodetic position computations)